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Assessing DEM interpolation methods for effective representation of upland stream morphology for rapid appraisal of bed stability

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4 **Assessing DEM interpolation methods for effective representation of**
5 **upland stream morphology for rapid appraisal of bed stability**
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ABSTRACT

Digital elevation models (DEMs) of river channels, built by interpolation between a sample of topographic survey points, are widely used to represent surfaces and to derive land-surface parameters. Differencing between successive DEMs permits quantification of change, which in gravel-bed rivers is used to construct a morphological budget of lower bound estimates of sediment flux and bed-stability surrogate. Choice of DEM interpolation method strongly influences DEM quality and realistic representation of channel forms. When comparing morphological budgets between multiple contrasting reaches, e.g. for rapid ecological appraisal, an effective and consistent means of DEM construction is required to avoid digitally generated inconsistencies. An appropriate interpolation method should be suitable for accurate representation of channels contrasting in substrate and hydraulic conditions, surveys of varying data density and distribution, and avoidance of site specific parameterisation. This paper investigates representation of channel form using a series of DEMs generated within Surfer[®] by triangulation with linear interpolation, natural neighbours, point kriging, universal kriging, multiquadratic radial basis function, modified Shepard's method and inverse distance to a power on the example in 4 reaches of mountain streams in New Zealand. These reaches represent a diversity of channel forms, substrate and hydraulic properties. DEMs from triangulation with linear interpolation revealed consistently the best results and this method is recommended for geomorphological and ecological studies of multiple reaches. The main advantage over point kriging and radial basis function is better representation of channel margins and bedforms without introduction of breaklines, while it outperforms natural neighbours in honouring measured points.

KEYWORDS

DEM, interpolation, morphological budgeting, Surfer, channel form, gravel-bed river, substrate stability, triangulation, kriging

INTRODUCTION

Fluvial geomorphology and hydrology can provide techniques and concepts that allow understanding of the complex hydrogeomorphological underpinnings of stream ecology (Poole, 2010). Consequently these disciplines share methods and tools, e.g. in geomorphology, hydrology and ecology DEMs are often used to represent topography or derive land-surface parameters. DEMs of riverine landscapes are of particular interest for mapping (e.g. pattern of morphological change), modelling (e.g. flow routing) and calculating of sediment budgets. Morphological changes and sediment budgets are determined from the difference in surface elevation of subsequent DEMs. Morphological budgeting is a widely applied and accepted method for quantifying areas of deposition or erosion and for determining lower-bound sediment fluxes within a gravel- and cobble-bed river reach (e.g. Ashmore and Church, 1998; Brasington *et al.*, 2000; Fuller *et al.*, 2005). In recent years the approach has shifted from budgets calculated from planform and/ or cross-sectional measurements (Brewer and Passmore, 2002; Fuller *et al.*, 2002; Martin and Church, 1995) to digital elevation model (DEM) based estimations (Brasington *et al.*, 2003; Chappell *et al.*, 2003; Eaton and Lapointe, 2001; Fuller *et al.*, 2003a; Fuller *et al.*, 2003b; Lane *et al.*, 1994; Westaway *et al.*, 2000).

The pattern of scour and fill within a reach identified for instance by morphological budgeting can be used in ecology to assess intensity and spatial extent of physical disturbance, to examine spawning habitat quality and to investigate the availability of stable refugia for stream organisms during floods (Matthaei and Townsend, 2000; Wheaton *et al.*, 2010a). Additionally sediment budgets at various scales (e.g. patch, riffle or entire reach) can be employed as a measure of bed stability (Schwendel *et al.*, in revision). Morphological budgeting also has the potential to replace scour chains in research on lotic ecosystems having the advantage of lower invasiveness and higher spatial resolution (Schwendel *et al.*, 2010a).

Surveys to collect data used to create DEMs can be airborne (e.g. photogrammetry, laser altimetry) (Brasington *et al.*, 2003; Ham and Church, 2000; Lane, 2001; Lane *et al.*, 2003; Westaway *et al.*, 2001) or ground based (photogrammetry, tacheometry, including, most recently, terrestrial laser scanning) (Fuller *et al.*, 2002; Heritage *et al.*, 1998; Lane *et al.*, 1994; Milan *et al.*, 2007) depending on the size of the reach and available technology. Airborne LiDAR and

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3 terrestrial laser scanning (TLS) can provide high resolution surveys but vegetation
4 (for LiDAR) and deeper water constrains application because of limited light
5 penetration of water. The latest generation of LiDAR overcomes the latter problem by
6 emitting also green light, which is not absorbed by water, but to date expense and
7 availability limit its application. More conventional techniques, such as terrestrial
8 tacheometry are widely available and more suitable for subaqueous surveys although
9 their lower resolution imposes some limits in assessment of surface roughness. This
10 needs to be accommodated by terrain sensitive data acquisition and a suitable DEM
11 interpolation method.
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19 Measurement of 3D coordinates on a surface is afflicted with several kinds of
20 error, notably precision, accuracy and reliability of measurements (Lane *et al.*, 1994).
21 Precision depends on the instruments used and surface roughness, while accuracy
22 describes systematic errors such as verticality of the survey pole (Lane *et al.*, 1994).
23 Gross errors or blunders control data reliability and are difficult to detect. Usually the
24 irregular network of surveyed points is transformed to a regular grid (interpolation)
25 which facilitates the comparison of DEMs from repeated surveys of the river bed.
26 However, this involves error associated with DEM accuracy (*sensu* Wood and Fisher,
27 1993) which is affected by the interpolation algorithm, spatial structure of altitude as
28 well as density and spatial distribution of data points (Brasington *et al.*, 2000; Chaplot
29 *et al.*, 2006; Desmet, 1997; Fisher and Tate, 2006). Hence selection of an appropriate
30 interpolation method can have a strong influence on resulting DEM quality (Erdogan,
31 2009; Heritage *et al.*, 2009; Kravchenko and Bullock, 1999; Wise, 2007; Yilmaz,
32 2007) but recommended methods vary with data density, scale and topography
33 (Chaplot *et al.*, 2006; Desmet, 1997).
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46 Environmental and ecological studies often require assessment of multiple
47 reaches of sometimes highly contrasting nature (e.g. Schwendel *et al.*, in revision).
48 This requires a straightforward generation of DEMs, ideally using the same
49 interpolation method for all reaches to provide consistency and improve comparability
50 between DEMs and derived parameters. Thus an appropriate interpolation method
51 should be suited to consistently generate DEMs that: (1) realistically and accurately
52 represent channels having a range of contrasting substrate and hydraulic conditions;
53 (2) are based on surveys of varying data density and distribution; (3) do not need time
54 consuming site specific adjustments such as development of semi-variograms or
55 introduction of breaklines; and (4) computation time should be manageable. This
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necessarily results in a trade-off between DEM quality of a single dataset and the suitability of a method for many datasets. The literature comprises many comparisons of site specific tailored interpolation methods (e.g. Desmet, 1997; Kravchenko and Bullock, 1999) and recent studies focus on development of new methodologies for data acquisition (e.g. Alho *et al.*, 2009; Hodge *et al.*, 2009), management of data uncertainty (e.g. Wheaton *et al.*, 2010a, b) and multi-scale data retrieval (e.g. Heritage *et al.*, 2009; McMillan and Brasington, 2007). In addition Heritage *et al.* (2009) have addressed the influence of survey strategy and performance of interpolation methods at a single site, but none of these studies has analysed the performance between contrasting channel environments. This study fills this gap which is important because it facilitates geomorphological and ecological research seeking to compare numerous, contrasting, river reaches and complies with the need of scientists to use morphological budgeting in applied and interdisciplinary studies.

This paper compares seven gridding methods on a range of topographic surveys of four diverse river reaches. DEMs were generated within Surfer[®], a spatial analysis software widely used for this purpose in geomorphology and other disciplines (e.g. Andrews *et al.*, 2002; Fuller and Hutchinson, 2007; Fuller *et al.*, 2003b; Pilesjö *et al.*, 2006; Schmidt and Persson, 2003; Takken *et al.*, 2001; Yilmaz, 2007). Dynamics of New Zealand headwater streams and processes responsible for the observed changes in topography are discussed elsewhere (Schwendel *et al.*, 2010b).

SITES AND METHODS

Sites

Between October 2007 and February 2008 two topographic surveys were completed at four mountain streams in the Ruahine and Tararua Ranges which are located in the southern part of New Zealand's North Island (Figure 1). The hydraulic properties of the reaches varied considerably in terms of slope, width and hydraulic radius as did sediment characteristics (Table I). Topographic characteristics range from relatively smooth, clearly structured gravel-bed streams with low surface roughness (Tamaki) to very bouldery streams with highly structured surfaces (Pukeatua) (Figure 2). Some reaches were laterally confined by vegetated banks (Manawatu) or valley topography (Pukeatua), whereas others migrated in wide floodplains (Tamaki, Waipawa). All catchments were dominated by native forest.

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For comparison of interpolation methods a sample of four surveys representing all four sites was selected (Table II). They cover a wide range of survey area and point density. Reach length was 5 – 7 times the recently active channel width in order to include at least one riffle-pool sequence (Keller and Melhorn, 1978; Leopold et al., 1964), however, where strong lateral channel migration seemed realistic a wider zone was surveyed.

Survey

The aim of the surveys was to generate DEMs from which morphological budgets of the gravel and cobble surface at a bedform scale could be constructed between successive dates. Budgets of this calibre of material are not only of commercial importance (e.g. gravel extraction) but also of ecological interest (e.g. providing an indication of stream bed stability, habitat change and physical disturbance).

Data were acquired using a differential GPS system (R8, Trimble Navigation Limited, Sunnyvale, USA) in RTK mode (cf. Brasington *et al.*, 2000). Where satellite reception was limited topographic data were retrieved with a electronic total station GTS 701 (Topcon Corporation, Tokyo, Japan). To prevent occurrence of multipath errors (Kennedy, 2002) the base station was installed some distance from each reach.

The survey was designed to be terrain sensitive, i.e. point density was highest at breaks in slopes and highly structured surfaces (Fuller *et al.*, 2005). Consequently in highly structured channels point density was higher than in smooth reaches. Substrates larger than cobbles require a grain scale resolution to be represented adequately in a DEM together with gravelly surfaces. As this is impractical for large survey areas, presence of boulders (b-axis >300 mm) was noted during the field survey and they were blanked in the DEM and thus not considered for budgeting. Concomitant tracking of in situ marked boulders showed that only 3% of them moved during floods. The surveyed surface reflects surface roughness, e.g. no attempt was made to measure at a grain-scale resolution and thus the survey pole was placed on top of stones as well as in gaps between particles. Surveyed areas vary between 132 m² and 2438 m² whereas average point density lies between 0.6 and 11.7 points m⁻² (Table II). Substrate composition was assessed with the Wolman pebble count method (Wolman, 1954) which measures the b-axis of >100 randomly selected substrate particles. They were classified according to a modified Wentworth scale and particle size fractions were calculated (Table I).

Precision of electronic theodolites or differential GPS systems is high, but due to satellite constellation, atmospheric interference or weather conditions larger errors can occur. These can be assessed with frequent measurements of independent check points during a survey (Brasington *et al.*, 2000) or more accurate data (Fisher and Tate, 2006). Internal quality control data generated by the survey device can also indicate precision of measurements (Fuller and Hutchinson, 2007). Here vertical precision calculated from a limited number of independent check points was 0.015 m which compares well to vertical error derived from internal quality control data ranging between 0.020 and 0.030 m. Survey error also depends on surface roughness and is often identified by a percentile of the substrate size distribution (Brasington *et al.*, 2000; Chappell *et al.*, 2003). Thus the 84th substrate size percentile of the surveyed bed material assemblage (upper threshold 300 mm) ($D_{84\text{corr}}$) provided an indicator for the error induced by surface roughness. The latter is significantly larger than the above identified instrument precision.

Interpolation

Data were analysed, interpolated and visualised with Surfer 8.01 (Golden Software, Golden, USA). A grid size of 0.1 m was chosen which is suitable to account for small scale variation in densely surveyed areas, but still large enough (compared to surface roughness and mean point distances) to avoid the occurrence of spurious artefacts (Brasington and Richards, 1998; Fuller *et al.*, 2003a). Modern software packages offer a wide range of local neighbourhood and geostatistical interpolation methods of which seven were tested: triangulation with linear interpolation, natural neighbours, point kriging without drift, universal kriging, multiquadratic radial basis function, modified Shepard's method and inverse distance to a power. These methods are briefly described in Chaplot *et al.* (2006), Franke (1982), Fuller *et al.* (2003a) and Yilmaz (2007). For the inverse power weighting a power of 2 with a search radius including maximal 64 points and no smoothing was applied. The very similar modified Shepard's approach used default values calculated in Surfer for the radii for quadratic fit and distance-weighting (Golden Software, 2002). Kriging was based on the default linear variogram with no nugget effect. All the tested interpolation methods except universal kriging are regarded as exact interpolators. This means the model honours the altitudes of surveyed points if these are lying on a grid node. Furthermore point kriging with linear drift (universal kriging) was also tested because

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3 a trend following the gradient of the stream was possible, at least for the larger
4 surveys (cf. Fuller *et al.*, 2003a). However, generally no anisotropy was assumed
5 because the length of the reaches was not much greater than the width. All methods
6 are within limits appropriate for irregularly distributed data. For all interpolation
7 methods the dataset specific default values generated in Surfer were used to keep the
8 analysis consistent and comparable. A specification of the gridding methods (e.g.
9 development of variograms for kriging, introduction of breaklines) for each dataset
10 might reveal better DEMs for a single survey but is not practicable with many datasets
11 and beyond the scope of this particular paper.
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19 20 21 *Comparison of interpolation methods and DEM quality*

22 Assessment of a DEM relative to the true surface requires more precise data of the
23 surface topography (Wise, 2007), but this is often not available. However,
24 independent topographic survey points can be used for total DEM error estimation if
25 the error in measurement of the check method is accounted for (Brasington *et al.*,
26 2003). Where independent data are unavailable, DEM quality can be explored using
27 split-sampling (Chaplot *et al.*, 2006; Desmet, 1997; Fisher and Tate, 2006), cross-
28 validation (Erdogan, 2009) or residual analysis (Fuller and Hutchinson, 2007; Fuller
29 *et al.*, 2003b; Yilmaz, 2007). Residual analysis uses non-independent data but has the
30 advantage over split-sample approaches of not reducing DEM quality, which is
31 important, since the survey was designed to be effective (terrain sensitive) and
32 provide the best possible data for interpolation (cf. Fuller and Hutchinson, 2007).
33 Quality assessment based on thinning of datasets works well with interpolation
34 methods that estimate a local surface as a function of many points (e.g. kriging), but
35 has disadvantages when a local surface depends only on a few neighbouring points
36 (e.g. triangulation). DEM quality is not only defined in terms of vertical accuracy but
37 also in terms of the desired application (e.g. DEM differencing) and derived
38 properties (e.g. slope) (Lane *et al.*, 2003; Wise, 2007). Derivatives like: slope;
39 curvature; estimation of change; or flow routing (Brasington and Richards, 1998;
40 Erdogan, 2009; Lane *et al.*, 2003; Wise, 2007) and comparisons between the DEM
41 and visual observations of the actual surface in check areas with certain properties
42 (e.g. planar surfaces, geometric bedforms) are often used to investigate shape
43 reliability (Desmet, 1997). Visualisation allows semi-quantitative assessment of the
44 DEM quality and is a common method to detect errors in DEMs (Desmet, 1997;
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3 Wood and Fisher, 1993). This is important regarding the purpose of the DEM (Fisher
4 and Tate, 2006): unlike DEMs for erosion or hydrological modelling, where
5 derivatives such as slope and flow routing are most important, DEMs for the purpose
6 of mapping, analysing spatial patterns of change or reach-wide sediment budgets need
7 to represent surfaces and channel shape realistically and close to the measured points.
8 For this reason visualisation techniques were employed to compare the performance
9 of different interpolation methods. In addition DEM error was investigated using
10 residual analysis and comparison with independently surveyed cross-sections.
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19 In a pre-selection phase models of all 4 datasets and each gridding method were
20 visualised with shaded relief maps and contour maps (c.f. Wood and Fisher, 1993).
21 These were qualitatively examined and interpolation methods that did not meet a
22 minimum level of realistic surface representation were excluded from further analysis.
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26 After consideration of linear drift in kriging models, a reduced number of
27 interpolation methods were tested according to the following criteria:
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- 29 (1) representation of relatively flat planes (e.g. depiction of sediment sheets or
30 channel armour),
 - 31 (2) representation of the surface of elevated grassy banks to depict their smooth and
32 stable character,
 - 33 (3) horizontal representation of straight lines (e.g. banks and bar margins),
 - 34 (4) vertical representation of channel margins (e.g. for assessment of channel cross-
35 profile),
 - 36 (5) representation of the channel bottom (e.g. gravel bars, pools and steps),
 - 37 (6) shape of contour lines to depict surface structure appropriately,
 - 38 (7) representation of longitudinal elements (e.g. continuity of bars, trenches and
39 banks) and
 - 40 (8) residual analysis (honouring the elevation of measured points).
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51 Additionally DEMs were compared directly (subtraction) with the triangulation
52 model chosen as a reference, because its generation is most intuitive. Differencing of
53 DEMs from two consecutive surveys was employed to investigate the use of different
54 methods in application of morphological budgeting. During visualisation only the
55 relative DEM quality between methods was assessed because survey precision was
56 not accounted for, however, this uncertainty is considered in the discussion.
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DEM quality was evaluated using mean error, standard deviation and mean absolute errors: The Mean Error (ME) is a commonly used measure which can account for the bias in data (systematic error) (Fisher and Tate, 2006) (Eq. 1) where n is the number of data points.

$$ME = \frac{\sum (Z_{survey} - Z_{DEM})}{n} \quad (1)$$

The standard deviation of the Mean Error (SD) records the magnitude of scatter around zero (Eq. 2).

$$SD = \sqrt{\frac{\sum [(Z_{survey} - Z_{DEM}) - ME]^2}{n - 1}} \quad (2)$$

Alternatively the Root Mean Square Error (RMSE) or the Mean Absolute Error (MAE) (Eq. 3) are used to assess the quality of a DEM. If the mean errors are close to zero RMSE and SD are similar, so only the MAE, ME and SD are discussed here.

$$MAE = \frac{\sum |Z_{survey} - Z_{DEM}|}{n} \quad (3)$$

It should be noted that the spatial variation in error was not accounted for in this study because for most methods only reach-averaged data were available.

RESULTS AND DISCUSSION

Pre-selection

Models of all 4 datasets and each gridding method were visualised with shaded relief maps and contour maps to rapidly appraise their representation of morphology relative to photographs. The triangulation, kriging, natural neighbours and radial basis function models show adequate representation of the channel surfaces. In contrast the modified Shepard's method produces an overly smooth surface even when no smoothing factor was employed and it also shows poor representation of linear

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3 features like channel margins. This is illustrated in the Manawatu dataset compared to
4 the triangulation model which served as a standard (Figure 3A and B). The DEM
5 created by inverse distance to a power contains many pointed holes and spiky features
6 on an otherwise smooth surface (Figure 3C). This can be adjusted by lowering the
7 power, but again the result is an over-smoothed topography and some spikes still
8 remain (Figure 3D). Thus in the pre-selection phase the modified Shepard's method
9 and inverse distance to a power were excluded from further analysis.

16 17 *Universal kriging*

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19 In a second step the influence of linear drift versus no drift for point kriging DEMs
20 was evaluated on all 4 datasets. The mean difference in residuals is only marginal
21 (less than 21 nm). The mean vertical difference between models of the channel is less
22 than ± 1 mm for the stronger small scale structured surveys Manawatu_2 and
23 Pukeatua_1 and less than ± 2 mm in the other two surveys. These differences lay far
24 below surface roughness (cf. Table I). This suggests that the influence of the slope of
25 the valley floor is negligible for surveys of such small longitudinal extent. Hence only
26 point kriging without linear drift is reported in the further evaluation of the methods to
27 avoid unnecessary duplication and detail.

34 35 36 37 *Criteria based comparison between methods*

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39 The remaining four interpolation methods triangulation with linear interpolation,
40 kriging, natural neighbours and radial basis function were subject to criteria based
41 analysis (Table III).

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46 *(1) Representation of relatively flat planes.* The active floodplain of Tamaki Stream
47 comprises some reasonably flat patches (Figure 2C in the background). There are no
48 large differences between DEMs, although natural neighbours, kriging and to a
49 certain extent radial basis function tend to create unrealistic island like concentric
50 shapes (bull's eyes) (Figure 4). The DEM generated with kriging seems to produce
51 the most even surface and the triangulation model seems to be most realistic in terms
52 of reproduction of longitudinal structures. No general ranking between these models
53 could be established for this criterion.

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(2) *Representation of the ground surface of elevated grassy banks.* Elevated grassy banks occur only on the Manawatu site (Figure 2B). Their surface is not even but quite regular. They were incorporated into the surveys to allow for lateral bank erosion and to define a stable boundary for surface interpolation. Point density is relatively coarse due to surface smoothness. Hence it is expected that DEMs represent a relatively flat surface between the points in order to avoid artificial differences between surveys of the same site.

The triangulation model and the natural neighbours DEMs (Figure 5A and B) give the impression of a plane bank as intended. In contrast the other two DEMs (Figure 5C and D) show an undulating surface with higher elevations between points in the longitudinal direction, a classical scalloping effect, also found by Fuller *et al.* (2003b). The DEM created with radial basis function demonstrates this behaviour also in lateral direction, thus it is the least appropriate interpolation method according to this criterion.

(3) *Horizontal representation of straight lines.* When linear features like channel margins were surveyed a point was measured at each bend so that the lines in between should be represented as straight lines. The northern channel bank at the Manawatu site (Figure 5) gives a good example of a very structured channel margin whereas the side walls of the Tamaki (Figure 4) and Waipawa sites are straighter. The performance of the different gridding methods is consistent throughout all these examples. The triangulation DEM (Figure 4A and Figure 5A) connects neighbouring points with a straight line as intended, but looks unrealistic and angular. The natural neighbours DEM (Figure 4B) produces slightly smoother shapes, which look more realistic and may have advantages with respect to the differencing of models over the edgy shapes of the triangulation DEM at the Manawatu site. The other two DEMs (Figure 4 and Figure 5) again show strong (radial basis function) and very strong (kriging) scallopy shapes between points and therefore do not represent linear features well.

(4) *Vertical representation of channel margins.* The vertical profile of channel margins is usually not straight but has a concave shape with a steeper upper part and a lower gradient at the base. Often the upper point could not be measured directly on the edge because the substrate was over loose. Thus the measured gradient was often

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3 lower than the actual slope. If further smoothing of the profile is applied during
4 modelling the displayed gradient might be too low and thus better represented by a
5 DEM using straight connections between measured points. Following this assumption
6 the triangulation DEM fits best (Figure 6A). The DEM created with radial basis
7 function gives the same gradient between points but it varies longitudinally along the
8 channel (Figure 6D). Kriging and natural neighbours generate slightly less steep
9 contours between points and kriging looks much smoother regarding the total channel
10 profile (Figure 6C and Figure 7C). This leads to the suggestion that over the whole
11 channel profile triangulation might give the best representation of actual cut-bank
12 slope but may overestimate the volume below the surface, which should be
13 recognised where bank erosion contributes to a morphological budget. Smoother bank
14 sections that are predominantly formed by depositional processes will be best
15 modelled with natural neighbours interpolation.
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28 *(5) Representation of the channel bottom.* Representation of the channel bottom is one
29 of the most important criteria because here the main changes in sediment budget are
30 likely to occur and bed stability can be detected. The channel bottom was often
31 surveyed in a regular grid between breaklines in surface topography; gravel bars,
32 banks and pools were accounted for with extra points. Thus a DEM should display the
33 latter structures realistically and not add features where they were not surveyed. This
34 is especially relevant for surveys with low point density (e.g. Waipawa_1).
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41 The area in Figure 7 depicts the wet channel and banks of the Waipawa River.
42 This section consists of an upstream run which leads into a riffle with a longitudinal
43 bar in the centre. Downstream follows an elongated pool. The model created with
44 radial basis function differs strongly from the others. It shows unrealistic peaks and
45 holes between measured points. Kriging and natural neighbours DEMs present some
46 bull's eyes, but beside that their representation of the channel floor is relatively
47 similar to that of the triangulation model. The longitudinal bar in the centre is best
48 modelled with triangulation.
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56 *(6) Shape of contour lines.* As contour line shapes reflect the surface structure, they
57 should resemble natural shapes in a channel. Kriging, natural neighbours and radial
58 basis function produce round shapes which are similar to real channel forms
59 (Figure 6). In case of the radial basis function derived DEMs the surface is often too
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3 pointy. The edgy appearance of the triangulated shapes shows little resemblance with
4 natural surface shapes and reflects the process of the Delaunay-triangulation (see also
5 Figure 5).
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11 (7) *Representation of longitudinal elements.* Longitudinal elements like bars, banks
12 and trenches need to be modelled as continuous feature and not as unconnected rows
13 of highs or lows. According to this criterion triangulation performs best, followed by
14 radial basis function DEMs (bars in centre of Figure 7A-D or bottom half of
15 Figure 4A-D). Natural neighbours and especially kriging often produce isolated bull's
16 eyes instead of longitudinal elements.
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23 (8) *Analysis of vertical residuals.* Deviation of the DEM surface from the measured
24 points is used as a relative measure for how well the interpolation honours the input
25 data. These DEMs showed generally very low deviations (Figure 8). The mean error
26 (Eq. 1) was negatively biased for radial basis function, natural neighbours and
27 triangulation whereas the values for kriging were weakly positive and the absolutely
28 lowest in comparison. The standard deviation of the ME (Eq. 2) varies considerably
29 between sites with no clearly recognisable connection to survey or site characteristics.
30 However, for each survey the magnitude of SD is similar for natural neighbours,
31 triangulation and kriging whereas the dispersion around the ME is much lower for
32 radial basis function. The mean absolute error (Eq. 3) shows a comparable distribution
33 with the exception that triangulation and kriging interchange their ranking. In
34 summary the MAE and SD of radial basis function DEMs were significantly lower
35 than these of the other models. Triangulation and kriging DEMs were close together
36 followed by the natural neighbours DEMs. Thus the analysis of residuals suggests use
37 of radial basis function as a preferential gridding method. It also shows that the
38 methods, although each regarded as exact interpolator, honour survey points to
39 varying degrees. Geostatistical methods such as kriging were suspected to perform
40 less well but showed similar results to a mathematically simple model like
41 triangulation. The spatial distribution of the residuals shows that the highest
42 differences occur for all DEMs on the channel margins, where the modelling is most
43 complicated (Figure 9).
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3 The criteria based on visualisation, rank triangulation with linear interpolation best
4 (except for contour shape), followed by the natural neighbours method (Table III). In
5 contrast, if just the residuals are considered the radial basis function performs much
6 better than the other methods. However, for the purpose of morphological budgeting it
7 is crucial that surfaces are represented as realistically as possible, not only at survey
8 points but also in between them. Thus triangulation with linear interpolation is the
9 most suitable and consistent method for gridding in a range of streambed
10 environments. This concurs with findings using different approaches to assess
11 interpolation at a single site (Fuller and Hutchinson, 2007; Heritage *et al.*, 2009).
12 Triangulation provides a robust technique which is unaffected by problems like over-
13 and undershooting of surfaces near a jump discontinuity (Gibbs phenomenon)
14 (Florinsky, 2002). Furthermore, triangulation with linear interpolation is favoured by
15 a terrain sensitive survey that has high point densities at breaks in surface slope. An
16 introduction of breaklines might have improved the performance of the other methods
17 but when dealing with multiple sites and datasets this would be time intensive.
18 However, the densification of survey points around breaks in slopes minimises this
19 problem.
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34 35 *Direct comparison*

36 The subtraction of the different DEMs from the triangulation DEM shows that the
37 channel is represented most consistently with differences mainly below ± 0.02 m
38 between the triangulation and the natural neighbours DEM for the Tamaki
39 (Figure 10A-C), Pukeatua (Figure 10D) and Manawatu sites. Kriging-generated
40 DEMs often show more than 0.02 m difference whereas the radial basis function
41 model exhibits the largest area of more than 0.02 m difference at these three sites.
42 This is also mirrored in the volumes of the void between the DEMs and the
43 comparison between cross-sections derived from DEMs and independent
44 measurements (Figure 11).
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53 At the Waipawa site kriging is closest to triangulation with differences mainly
54 below 0.05 m. The natural neighbours DEM lies within a vertical distance of mostly
55 less than 0.1 m. In contrast the deviation of the radial basis function DEM is in some
56 areas considerable. As the Waipawa_1 survey has the lowest point density, the change
57 in performance relative to triangulation could be related to that.
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3 Overall the differences between models are smallest at the Tamaki site (Figure 11)
4 which possesses the lowest surface roughness and few small-scale structures. Here the
5 deviations from the triangulation occur mainly at the channel margins and to a lesser
6 extent on the channel bottom and floodplain ($< \pm 0.02$ m) (Figure 10A-C). In contrast
7 differences between methods are more likely to appear at the channel bottom at
8 reaches which are highly structured on a small scale like the Pukeatua site
9 (Figure 10D). This leads to the conclusion that there is no general bias between the
10 methods although the residuals of the DEMs show a small variation in magnitude and
11 direction. Differences between methods are consequently apparent only at small-scale
12 structures and little when compared to surface roughness. The latter is the dominant
13 error component afflicting data acquisition and of similar magnitude than
14 interpolation errors (Schwendel *et al.*, 2010b). Thus an adequate detection threshold
15 can to some degree account for inappropriate model choice.
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28 *Comparison in application*

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30 The Tamaki and to a slightly lesser extent Waipawa sites can be regarded as showing
31 responsive behaviour to small and intermediate floods reflecting a degree of intrinsic
32 coupling. Abundant and highly erodible sediments from steep catchments with high
33 erosion rates result in combination with frequent floods in a low channel and substrate
34 stability (Schwendel *et al.*, 2010b). At these reaches DEM differencing is unlikely to
35 detect effects caused by interpolation methods because it is masked by actual surface
36 changes. Hence only the more stable Manawatu site is displayed (Figure 10). All
37 methods show the highest change in topography at the channel margins. This could be
38 due to lateral erosion (often locally initiated by grazing cattle and sheep) or an artefact
39 of interpolation. The fact that it appears almost on the entire southern bank, points
40 towards the latter because no large scale bank erosion was visible there (Figure 2B).
41 Patterns of scour and fill are similar between the methods with the exception that the
42 radial basis DEMs exhibit less scour and fewer zones of no change in the channel.
43 The triangulation DEM shows the smallest volume of change (Figure 12) but within
44 the same order as kriging and natural neighbours. The major source of this
45 discrepancy seems to be representation of the channel margin.
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CONCLUSIONS

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Suggestions of optimal interpolation method from previous investigations are equivocal and subjective (Desmet, 1997) and are only valid for certain scales and surface characteristics. However, geomorphological and ecological studies that seek efficient and consistent comparison of sediment budgets derived by DEM differencing between numerous rivers require an interpolation method that allows a realistic representation of the topography of contrasting channels and can deal with varying data density and distribution. Furthermore, a large number of datasets favours approaches that do not need much site-specific parameterisation. This study accounts for these constraints at a river reach scale.

From the range of exact interpolation methods offered in Surfer[®], triangulation with linear interpolation modelled the varying surfaces and channel shapes most realistically and consistently without the need to introduce breaklines or site specific parameters. It appears that this mathematically simple method is well suited for terrain sensitive surveys and the range of point densities investigated. Under these conditions triangular artefacts are rare and it produces superior results to geostatistical and other local neighbourhood approaches.

Triangulation with linear interpolation is commonly used for generation of DEMs of single sites (e.g. Brasington *et al.*, 2003; Brasington *et al.*, 2000; Fuller and Hutchinson, 2007; Heritage *et al.*, 2009) but it is also very suitable for comparative studies of multiple river reaches with contrasting channel topographies. This leads to the recommendation of triangulation with linear interpolation as a comprehensive and reliable method of DEM generation for environmental and ecological studies that aim to assess spatial variation in erosion and deposition at various scales and for investigation in bed stability between several varying coarse-substrate streams.

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Table I. Hydraulic and substrate characteristics of the study reaches

site	Stream order (Strahler, 1952)	Slope (m^*m^{-1})	Mean hydraulic radius at bankfull (m)	Mean bankfull width (m)	Mean substrate D_{50} (mm)	Substrate composition (in order of relative proportion of s - sand, g - gravel, c - cobbles, b - boulders)
Waipawa	3	0.032	0.481	48.6	58.5	g, c, b
Manawatu	3	0.047	0.232	7.4	64.9	c, g, b
Tamaki	2	0.021	0.195	19.0	35.2	g, c
Pukeatua	3	0.047	0.912	24.2	83.9	c, g, b

Table II. Point density and survey area of all surveys between October 2007 and May 2008 (datasets selected for testing interpolation methods are in bold)

survey	1 (October/ November 2007)		2 (January/ February 2008)	
site	area (m^2)	point density (m^{-2})	area (m^2)	point density (m^{-2})
Waipawa	1897.22	0.58	2437.94	1.54
Manawatu	131.84	9.41	159.69	11.73
Tamaki	902.64	2.05	886.20	3.86
Pukeatua	613.49	1.95	1002.41	2.11

Table III. Summary of the evaluation of criteria and ranking in brackets (1 – most suitable, 4 – least suitable)

Criterion	Triangulation	Natural neighbours	Kriging	Radial basis function
(1) planes	Flat (1)	Flat (1)	Flat (1)	Flat (1)
(2) banks	Flat (1)	Flat (1)	Undulating (3)	Undulating (4)
(3) horizontal lines	Straight (2)	Realistic (1)	Very scallopy (4)	Scallopy(3)
(4) channel margins	Steep, straight (1)	Smooth (3)	Smoother (4)	Steep, smooth (2)
(5) channel bottom	Realistic (1)	OK (2)	OK (2)	Poor (4)
(6) Contours	Angular (4)	Round (1)	Round (1)	Round, deep (3)
(7) longitudinal elements	Realistic (1)	Isolated peaks (3)	Spiky (4)	Single peaks (2)
(8) residuals	OK (2)	Highest (4)	OK (2)	Lowest (1)
Sum of ranks	13	16	21	20

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5 **Figure 1.** Study sites in the southern part of the North Island of New Zealand.
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9 **Figure 2.** Study reaches: Waipawa (A), Manawatu (B), Tamaki (C) and Pukeatua (D).
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12 **Figure 3.** DEMs of survey Manawatu_2 generated with modified Shepard's method
13 (A), triangulation with linear interpolation (B), inverse distance to a power of 2 (C)
14 and inverse distance to a power of 1 (D). Arrow indicates flow direction and
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16 coordination axes denote easting and northing in m.
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21 **Figure 4.** Comparison of representation of relatively flat patches of the Tamaki
22 floodplain between gridding methods: triangulation (A), natural neighbours (B),
23 kriging (C), radial basis function (D). The distance between contour lines is 0.02 m.
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28 **Figure 5.** Comparison of representation of the banks and channel margins at the
29 Manawatu site between gridding methods: triangulation (A), natural neighbours (B),
30 kriging (C), radial basis function (D). The distance between contour lines is 0.1 m,
31 measured points are displayed as crosses.
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37 **Figure 6.** Comparison of representation of the channel margins at the Tamaki site
38 between gridding methods: triangulation (A), natural neighbours (B), kriging (C),
39 radial basis function (D). The distance between contour lines is 0.02 m, measured
40 points are displayed as crosses.
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46 **Figure 7.** Comparison of representation of the channel bottom at the Waipawa site
47 between gridding methods triangulation: (A), natural neighbours (B), kriging (C),
48 radial basis function (D). The distance between contour lines is 0.05 m, measured
49 points are displayed as crosses and an arrow indicates flow direction.
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55 **Figure 8.** Residual analysis: mean error (ME) with error bars indicating the standard
56 deviation (SD) and mean absolute error (MAE) (symbols) between sites and gridding
57 methods
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4 **Figure 9.** Spatial distribution of vertical residuals of models generated with
5 triangulation (A), natural neighbours (B), kriging (C) and radial basis function (D) for
6 the Manawatu_2 dataset. Arrow indicates flow direction and coordination axes denote
7 easting and northing in m.
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12 **Figure 10.** Subtraction of models generated with kriging (A), radial basis function (B)
13 and natural neighbours (C, D) from triangulation model for Tamaki_2 (A-C) and
14 Pukeatua_1 datasets (D). Arrow indicates flow direction and coordination axes denote
15 easting and northing in m.
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21 **Figure 11.** Cross-sections derived from different DEMs and independent topographic
22 measurements (“cross-section”): Tamaki (A), Manawatu (B). Shaded areas depict
23 blanked sections in the DEMs because of the presence of boulders (visible at the
24 independent cross-section). Deviations between models and from independent surveys
25 are more accentuated at small-scale structured sites (Manawatu) than at smoother
26 surfaces (Tamaki) but are small compared to survey precision as defined by surface
27 roughness (e.g. D_{84} is 0.058 m and 0.158 m at Tamaki and Manawatu respectively).
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35 **Figure 12.** Models of change between the datasets Manawatu_1 and Manawatu_2
36 generated with triangulation (A), natural neighbours (B), kriging (C) and radial basis
37 function (D). Arrow indicates flow direction and coordination axes denote easting and
38 northing in m.
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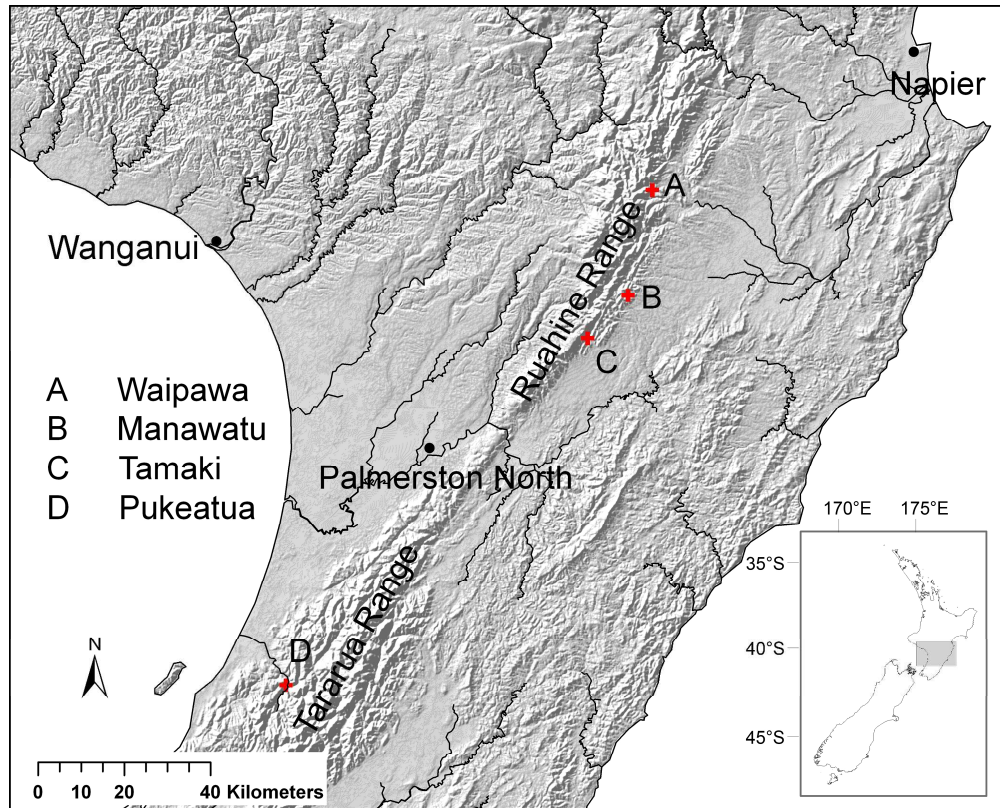


Figure 1. Study sites in the southern part of the North Island of New Zealand.
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Review

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Figure 2. Study reaches: Waipawa (A), Manawatu (B), Tamaki (C) and Pukeatua (D).
170x127mm (600 x 600 DPI)

Review

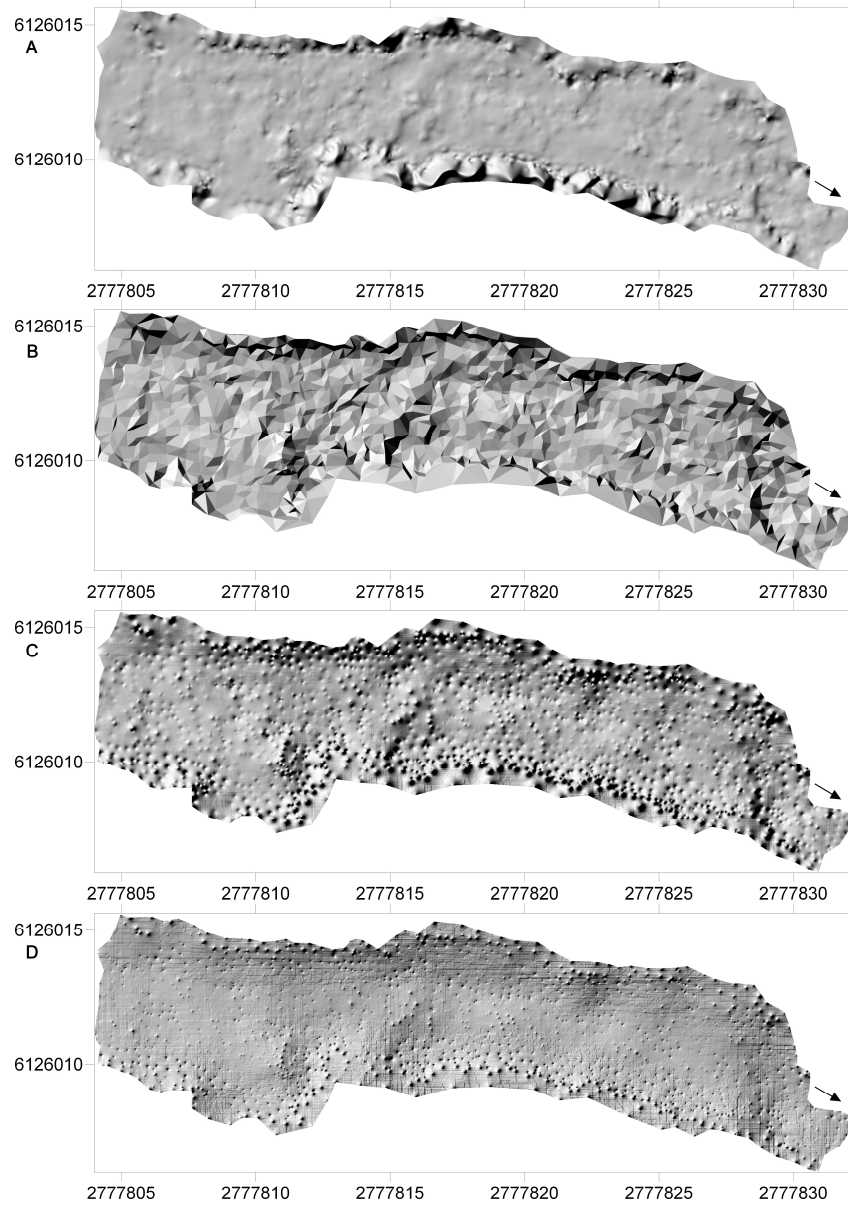


Figure 3. DEMs of survey Manawatu_2 generated with modified Shepard's method (A), triangulation with linear interpolation (B), inverse distance to a power of 2 (C) and inverse distance to a power of 1 (D). Arrow indicates flow direction and coordination axes denote easting and northing in m. 170x241mm (600 x 600 DPI)

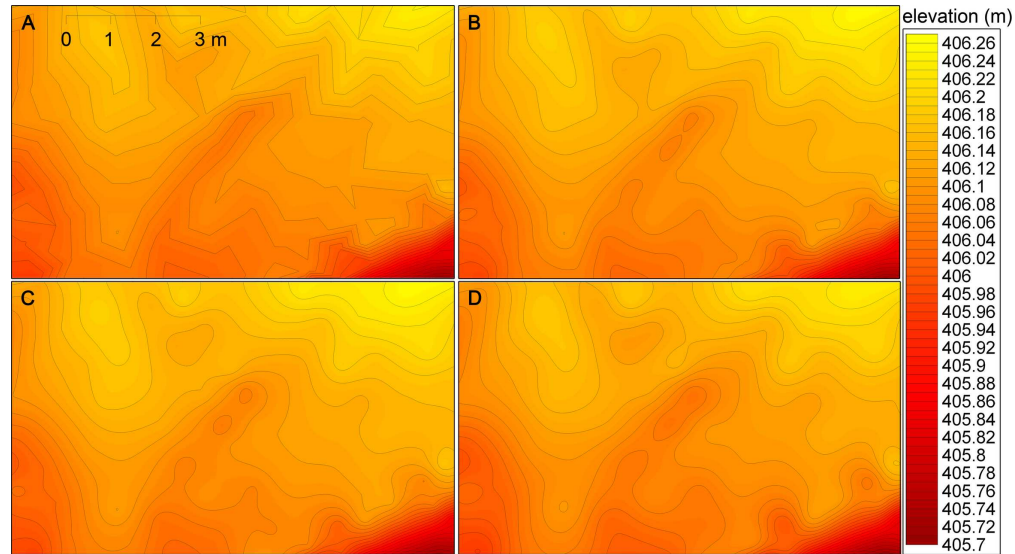


Figure 4. Comparison of representation of relatively flat patches of the Tamaki floodplain between gridding methods: triangulation (A), natural neighbours (B), kriging (C), radial basis function (D). The distance between contour lines is 0.02 m. 98x54mm (600 x 600 DPI)

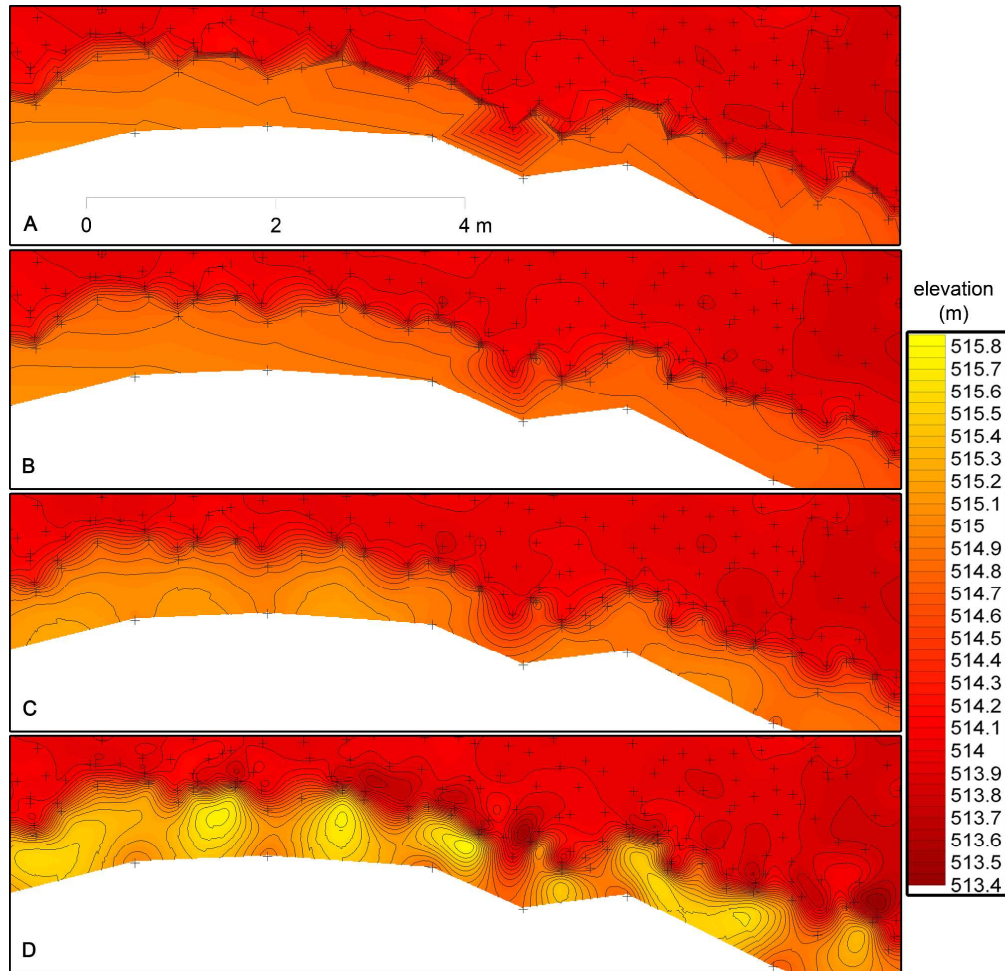


Figure 5. Comparison of representation of the banks and channel margins at the Manawatu site between gridding methods: triangulation (A), natural neighbours (B), kriging (C), radial basis function (D). The distance between contour lines is 0.1 m, measured points are displayed as crosses.
170x165mm (600 x 600 DPI)

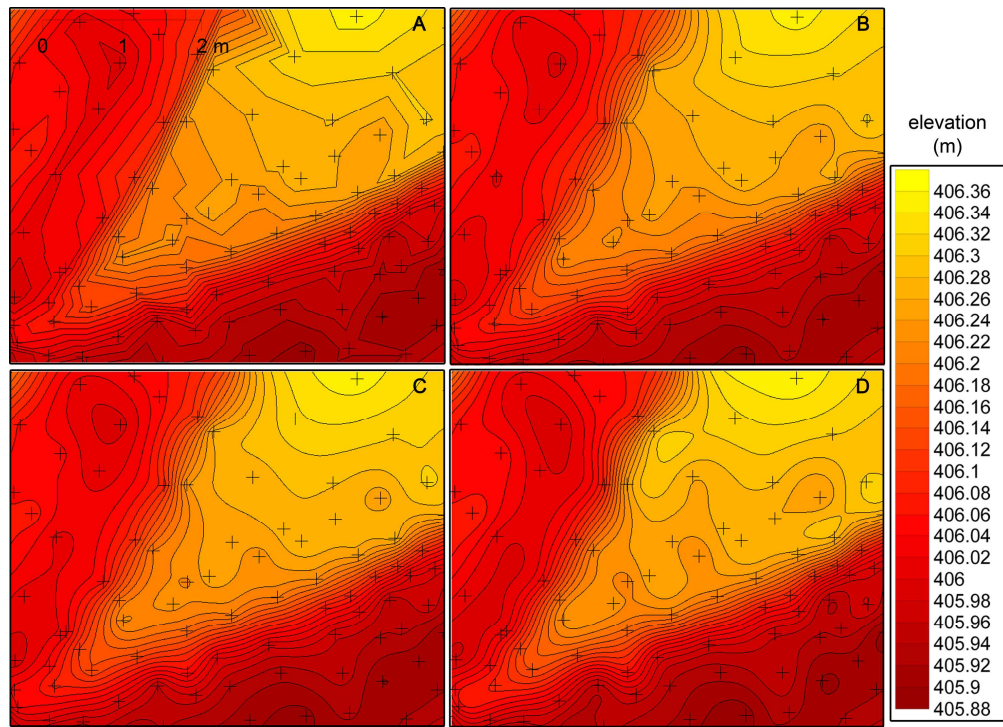


Figure 6. Comparison of representation of the channel margins at the Tamaki site between gridding methods: triangulation (A), natural neighbours (B), kriging (C), radial basis function (D). The distance between contour lines is 0.02 m, measured points are displayed as crosses. 129x93mm (600 x 600 DPI)

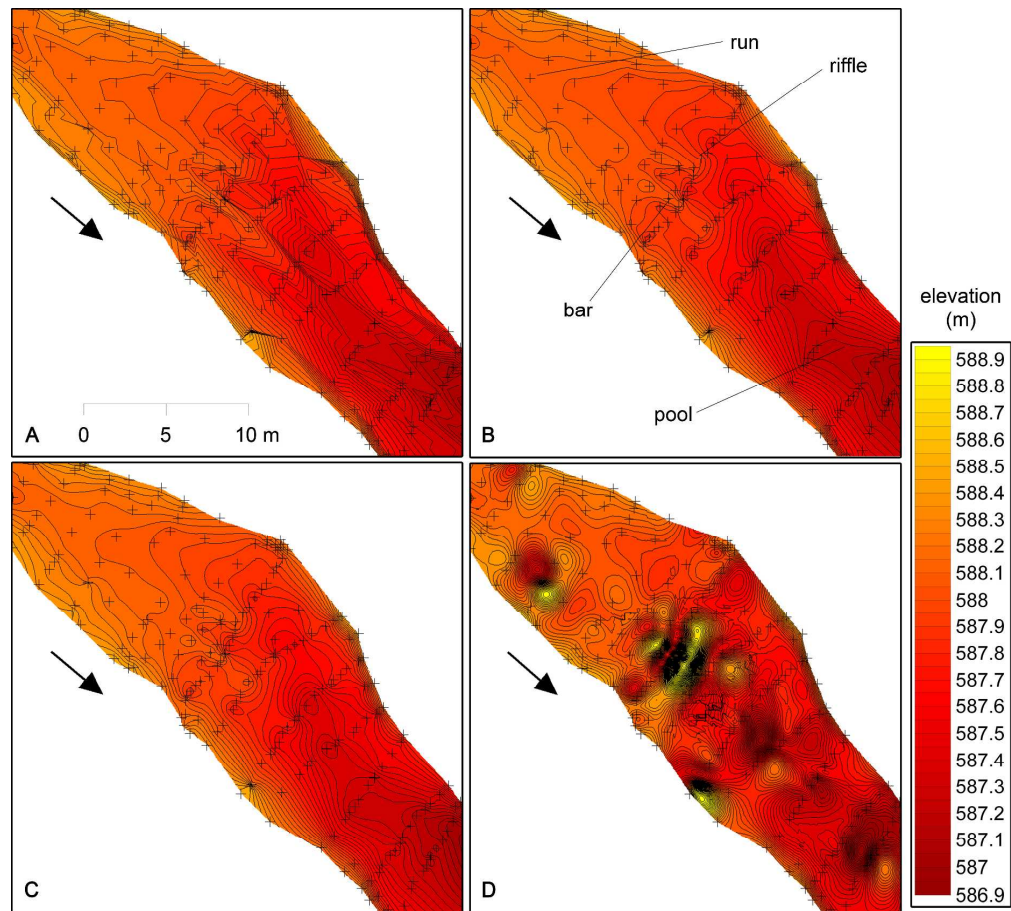


Figure 7. Comparison of representation of the channel bottom at the Waipawa site between gridding methods triangulation: (A), natural neighbours (B), kriging (C), radial basis function (D). The distance between contour lines is 0.05 m, measured points are displayed as crosses and an arrow indicates flow direction.
157x142mm (600 x 600 DPI)

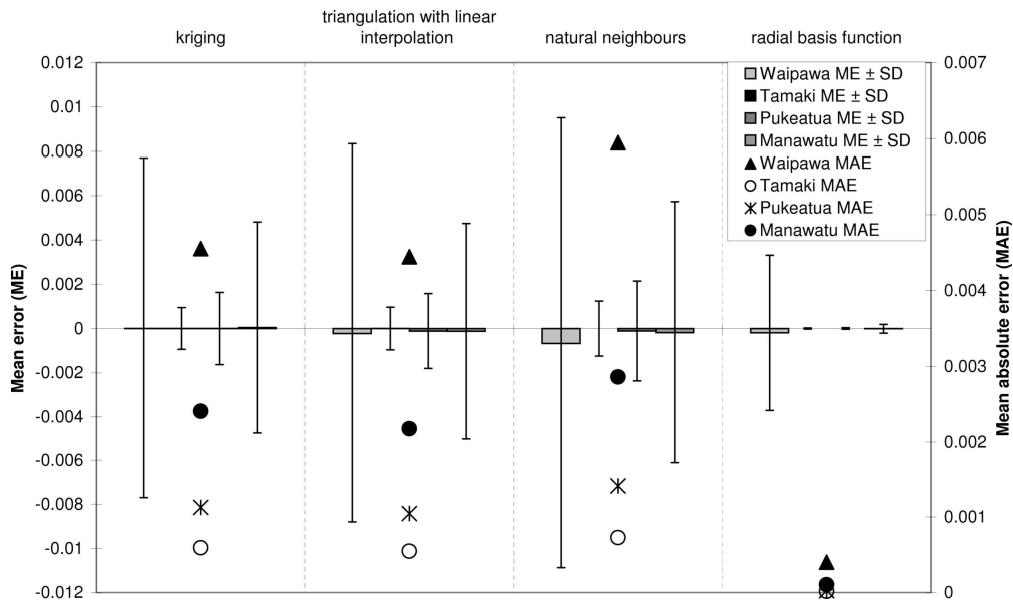


Figure 8. Residual analysis: mean error (ME) with error bars indicating the standard deviation (SD) and mean absolute error (MAE) (symbols) between sites and gridding methods 106x62mm (600 x 600 DPI)

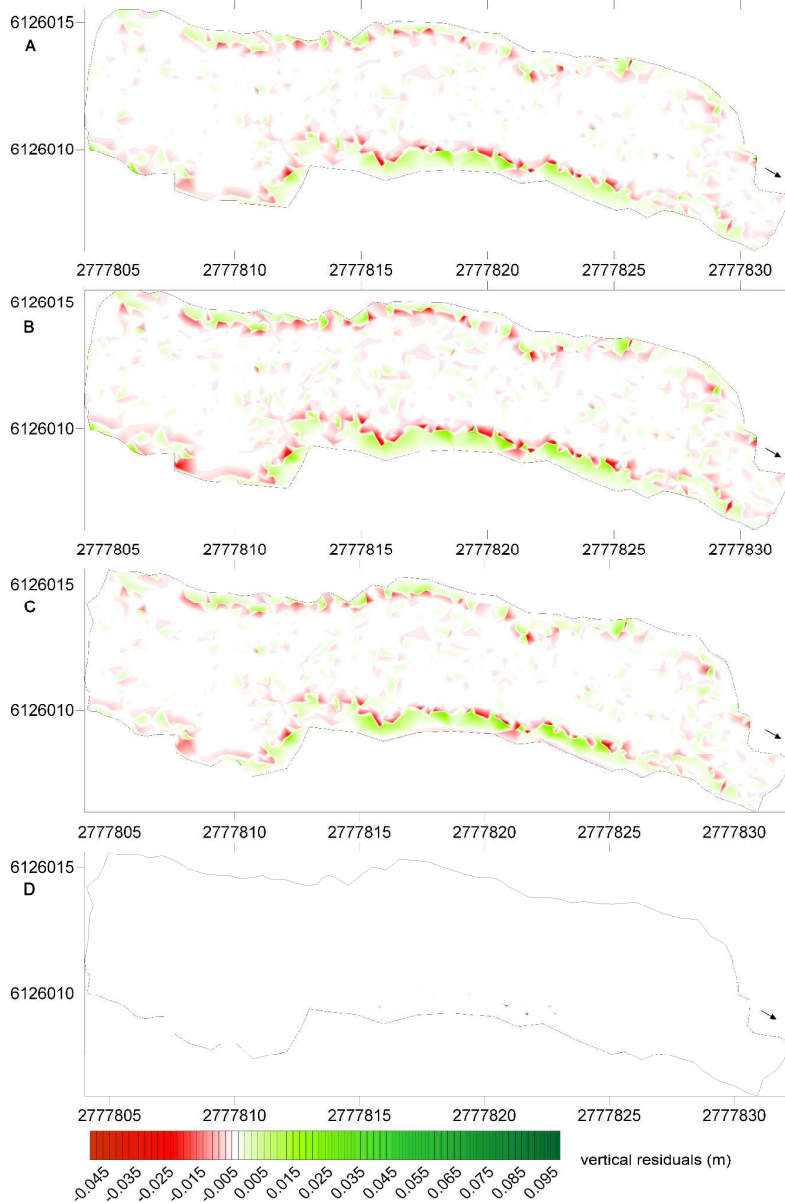


Figure 9. Spatial distribution of vertical residuals of models generated with triangulation (A), natural neighbours (B), kriging (C) and radial basis function (D) for the Manawatu_2 dataset. Arrow indicates flow direction and coordination axes denote easting and northing in m. 170x258mm (600 x 600 DPI)

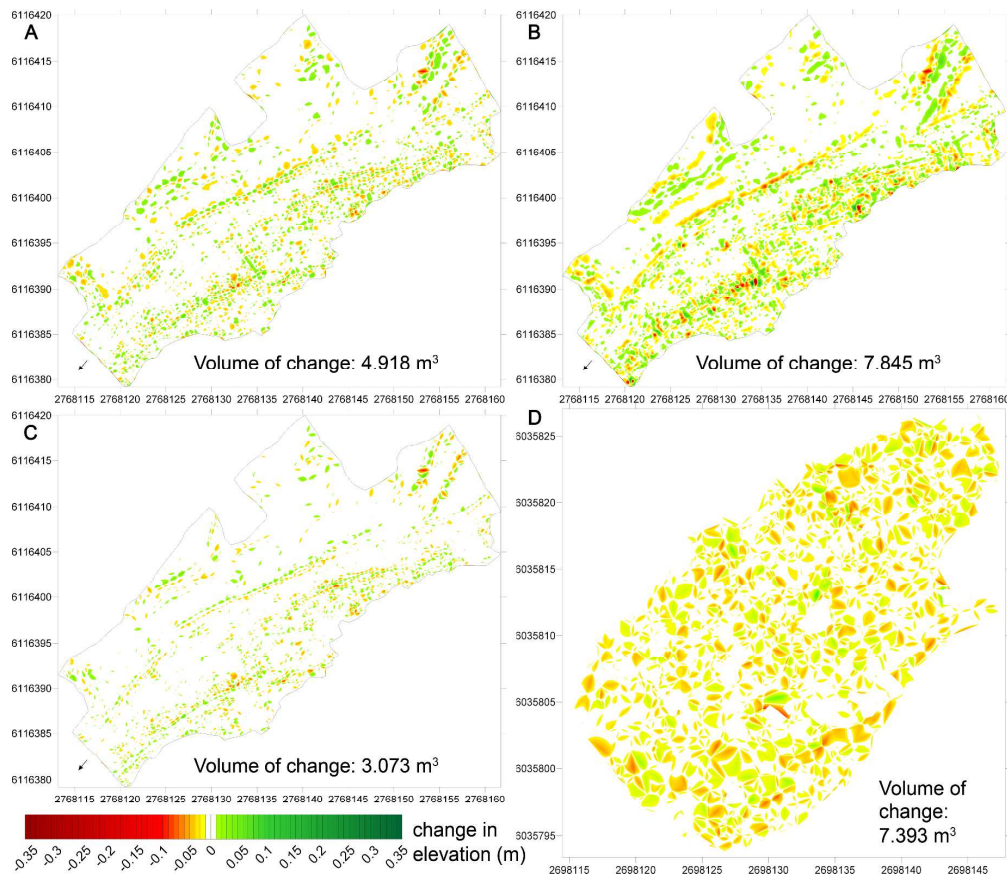


Figure 10. Subtraction of models generated with kriging (A), radial basis function (B) and natural neighbours (C, D) from triangulation model for Tamaki_2 (A-C) and Pukeatua_1 datasets (D). Arrow indicates flow direction and coordination axes denote easting and northing in m. 155x134mm (600 x 600 DPI)

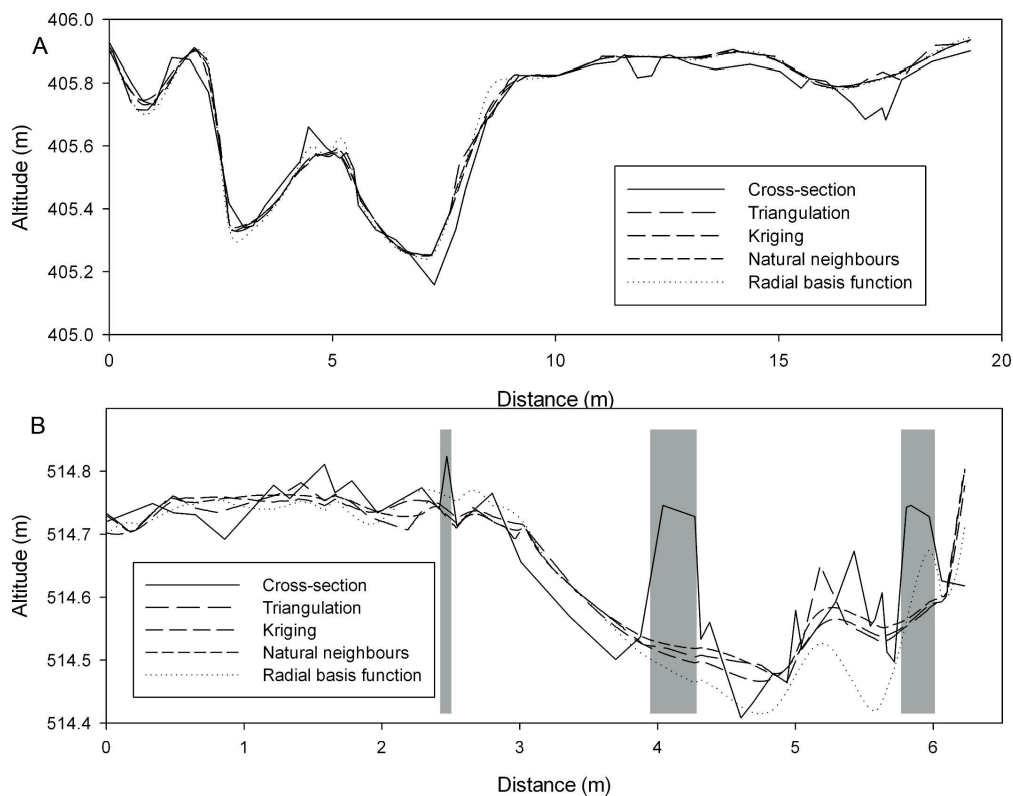


Figure 11. Cross-sections derived from different DEMs and independent topographic measurements ("cross-section"): Tamaki (A), Manawatu (B). Shaded areas depict blanked sections in the DEMs because of the presence of boulders (visible at the independent cross-section). Deviations between models and from independent surveys are more accentuated at small-scale structured sites (Manawatu) than at smoother surfaces (Tamaki) but are small compared to survey precision as defined by surface roughness (e.g. D84 is 0.058 m and 0.158 m at Tamaki and Manawatu respectively).

180x140mm (600 x 600 DPI)



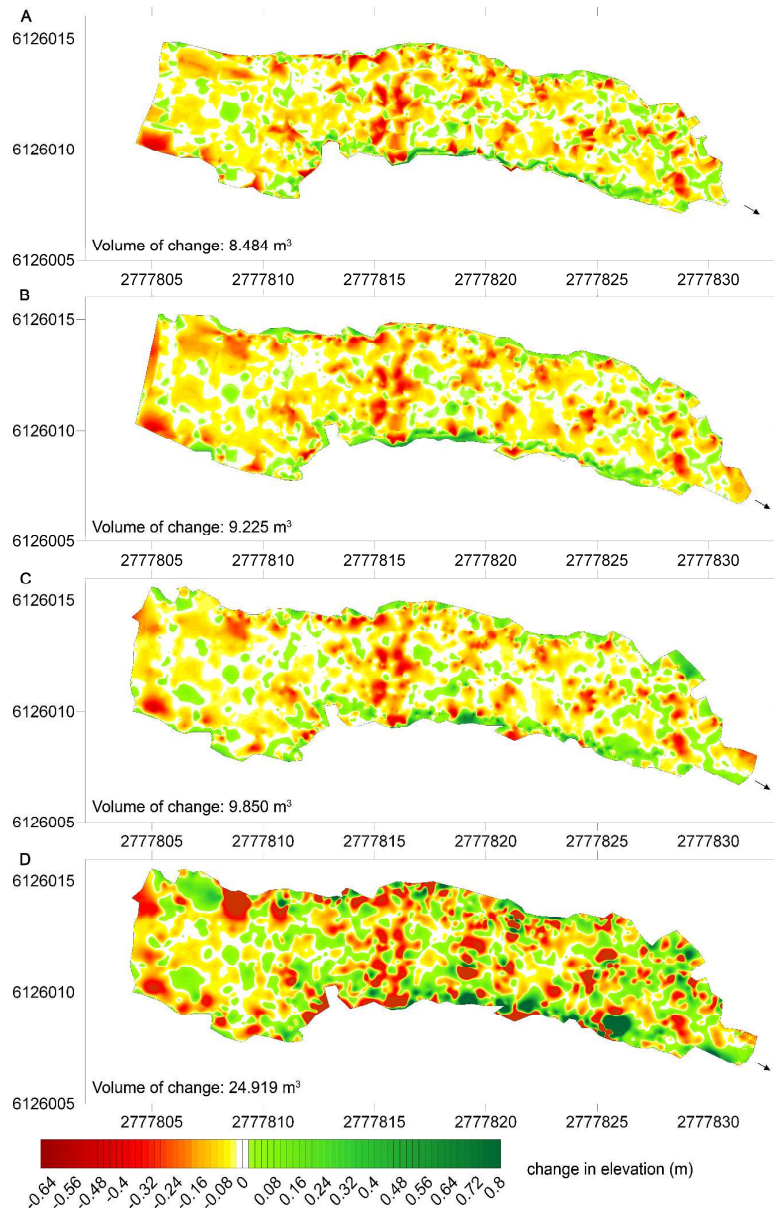


Figure 12. Models of change between the datasets Manawatu_1 and Manawatu_2 generated with triangulation (A), natural neighbours (B), kriging (C) and radial basis function (D). Arrow indicates flow direction and coordination axes denote easting and northing in m.
170x265mm (600 x 600 DPI)